

Honors Final Review

Part I: Define/explain the following terms/concepts.

1. Newton's Universal Law of Gravitation  $\rightarrow F_g$  is proportional to the product of the masses and inversely proportional to the square of the distance between them
2. "Weightlessness" in orbit  $\rightarrow$  in orbit you feel weightless since you are in constant free fall about the planet.
3. Work  $\rightarrow$  work is done when a <sup>1</sup> force <sup>2</sup> causes a <sup>3</sup> displacement.  $W = F \Delta x \cos \theta$
4. Power  $\rightarrow$  The rate at which work is done.  $P = W/t$
5. Force vs. Displacement Graphs  $\rightarrow$  The area under the curve is the work done by the force
6. Energy  $\rightarrow$  The ability to do work
7. Kinetic Energy  $\rightarrow$  The energy of an object in motion
8. Potential Energy  $\rightarrow$  The energy of an object due to its vertical position
9. Work-Energy Theorem  $\rightarrow$  The work done equals an object's change in KE.  $W = \Delta KE$
10. Law of conservation of energy  $\rightarrow$  Energy can be transformed from one kind to another, but the total energy never changes.
11. Momentum (definition and units)  $\rightarrow$  The product of mass and velocity;  $\text{kg} \cdot \text{m/s}$  or  $\text{N} \cdot \text{s}$
12. Law of conservation of momentum  $\rightarrow$  momentum is always conserved in a closed, isolated system (no external forces)
13. Impulse (definition and units)  $\rightarrow \vec{J} = \vec{F} \cdot t = \Delta \vec{p}$ ; units are the same as momentum
14. Center of mass  $\rightarrow X_{cm} = \frac{1}{M} \sum x_i m_i$ ; You do not need mass at the C.O.M.
15. Inelastic Collisions  $\rightarrow$  KE is NOT conserved; In a perfectly elastic collision the objects stick together.
16. Elastic Collisions  $\rightarrow$  No loss of KE; objects bounce off one another
17. Force vs Time Graphs  $\rightarrow$  Area under curve is the ~~work~~ impulse or  $\Delta \vec{p}$
18. Angular displacement  $\rightarrow \Delta \theta = s/r$
19. Angular velocity  $\rightarrow \omega = \Delta \theta / \Delta t$
20. Angular acceleration  $\rightarrow \alpha = \Delta \omega / \Delta t$
21. Torque  $\rightarrow$  torque is analogous to force;  $\tau = I \alpha = r F \sin \theta$
22. Moment of Inertia  $\rightarrow$  analogous to mass; an object's resistance to a change in rotation
23. Newton's Second Law for Rotation  $\rightarrow \sum \tau = I \alpha$

\*NOTE! Be careful with units in rotation problems. Formulas typically require radians.

Part II: Solve the following problems.

1. The radius of the earth is approximately  $6.38 \times 10^6 \text{ m}$  and the mass is approximately  $5.97 \times 10^{24} \text{ kg}$ . What is the acceleration due to gravity at a height of  $8.5 \times 10^6 \text{ m}$ ?

$$F_g = \cancel{mg} = G \frac{m_1 m_2}{r^2} \quad \text{Total distance from center of earth.}$$

$$g = 6.67 \times 10^{-11} \left( \frac{5.97 \times 10^{24}}{(6.38 \times 10^6 + 8.5 \times 10^6)^2} \right) = \boxed{1.798 \text{ m/s}^2}$$

2. Calculate the gravitational force exerted on a 3500 kg satellite orbiting 10,000 km from earth (mass  $5.97 \times 10^{24} \text{ kg}$ ).

$$F_g = G \frac{m_1 m_2}{r^2} = 6.67 \times 10^{-11} \left( \frac{3500 (5.97 \times 10^{24})}{(10,000,000 + 6.38 \times 10^6)^2} \right)$$

$$\boxed{F_g = 5194.46 \text{ N}}$$

3. Calculate the amount of work required to raise a 10 kg object 3 m above the ground.

$$W = F \Delta x \cos \theta$$

$$= mg \Delta x \cos \theta$$

$$= 10(9.8)(3) \cos 0^\circ \Rightarrow \boxed{W = 294 \text{ J}}$$

4. Calculate the amount of work required to stop a 25 kg object traveling at 8 m/s.

$$W = \Delta KE$$

$$= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$= \frac{1}{2} (25)(0^2) - \frac{1}{2} (25)(8)^2 \rightarrow \boxed{W = -800 \text{ J}}$$

5. A 5 kg cannon ball traveling 30 m/s creates a crater 2 m deep. What is the average force exerted by the cannon ball on the ground?

$$W = \Delta KE = F \Delta x \cos \theta$$

$$\frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 = F \Delta x \cos \theta$$

$$- \frac{1}{2} (5)(30)^2 = F(2) \cos 180^\circ$$

$$\boxed{F = 1125 \text{ N}}$$

Ground exerts an upwards force while the displacement is down so  $\theta = 180^\circ$

6. A box sliding on a frictionless surface at 15 m/s encounters a hill. How far up the hill will it slide?

$$KE_i = PE_f$$

$$\frac{1}{2} \cancel{mv^2} = \cancel{m}gh$$

$$\frac{1}{2}(15)^2 = 9.8h \rightarrow \boxed{h = 11.47\text{m}}$$

7. A disk with a diameter of 15 cm is rolling at 15 m/s encounters a hill. How far up the hill will it slide?

$$KE_t + KE_r = PE_f$$

$$\frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = mgh$$

$$\frac{1}{2} \cancel{mv^2} + \frac{1}{2} \left( \frac{1}{2} \cancel{m} \right) \left( \frac{v^2}{\cancel{r}} \right) = \cancel{m}gh$$

$$\frac{1}{2}(15)^2 + \frac{1}{4}(15)^2 = 9.8h \rightarrow \boxed{h = 17.219\text{m}}$$

- ★ 8. An object is launched off a 20m tall ledge with an initial velocity of 5 m/s. What is the speed of the object upon impact?

$$PE_i + KE_i = KE_f$$

$$\cancel{m}gh + \frac{1}{2} \cancel{mv^2} = \frac{1}{2} \cancel{mv^2}$$

$$9.8(20) + \frac{1}{2}(5)^2 = \frac{1}{2}v^2 \rightarrow \boxed{v = 20.42\text{m/s}}$$

9. A car traveling 10 m/s collides with an equal mass car at rest. If the cars stick together after the collision, what is the final speed they will travel?

$$\vec{P}_i = \vec{P}_f$$

$$m_1v_1 = (m_1 + m_2)v'$$

$$\cancel{m}v_1 = 2\cancel{m}v' \rightarrow \boxed{v' = 5\text{m/s}}$$

10. A cat jumps on a skateboard traveling at 15 m/s. If the mass of the cat and skateboard is 35 kg and they travel at 10 m/s, what is the mass of the cat?

$$\vec{P}_i = \vec{P}_f$$

$$\cancel{m_c}v_c + m_s v_s = (m_c + m_s)v'$$

$$m_s(15) = 35(10)$$

$$m_s = 23.33\text{kg}$$

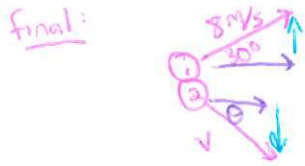
$$35 = m_c + m_s$$

$$35 = m_c + 23.33$$

$$\boxed{m_c = 11.66\text{kg}}$$



11. A pool ball traveling 10 m/s collides head on with a pool ball at rest. If they have the same mass and the first ball travels at 8 m/s at a 30 degree angle above the horizontal, how fast and in what direction does the second ball travel?



y direction:  $P_i = P_f$   
 $0 = m_1 v_{1y} + m_2 v_{2y}$   
 $v_{1y} = -v_{2y}$   
 $8 \sin 30 = -v_{2y}$   
 $v_{2y} = 4 \text{ m/s } \hat{y}$

x direction:  $m_1 v_i = m_1 v_{1x} + m_2 v_{2x}$   
 $10 = 8 \cos 30 + v_{2x}$   
 $v_{2x} = 3.07 \text{ m/s}$

$v = \sqrt{3.07^2 + 4^2} = 5.043 \text{ m/s}$   
 $\theta = \tan^{-1}(4/3.07) = 52.48^\circ$

12. Is the situation described in number 11 a perfectly elastic collision?

initial KE:  $\frac{1}{2} m v^2 = \frac{1}{2} m (10)^2 = 50m \text{ J}$

final KE:  $\frac{1}{2} m v^2 + \frac{1}{2} m v^2 = \frac{1}{2} m (8)^2 + \frac{1}{2} m (5.043)^2 = 44.7m \text{ J}$

Since KE is lost, it is NOT a perfectly elastic collision.

13. A wheel rotates at 1500 rpm. What is its angular velocity in radians per second?

$\frac{1500 \text{ rev}}{\text{min}} \times \frac{1 \text{ min}}{60 \text{ sec}} \times \frac{2\pi \text{ rad}}{1 \text{ rev}} = 157.08 \text{ rad/sec}$

14. A record player is turned on from rest and accelerates at  $1.23 \text{ rad/s}^2$ . What is its speed after 2.8 seconds in rpm?

$\omega_i = 0 \text{ rad/sec}$   
 $\alpha = 1.23 \text{ rad/s}^2$   
 $t = 2.8 \text{ sec}$

$\omega_f = \omega_i + \alpha t$   
 $= 0 + 1.23(2.8)$   
 $\omega_f = 3.444 \text{ rad/s} \times \frac{60 \text{ sec}}{1 \text{ min}} \times \frac{1 \text{ rot}}{2\pi \text{ rad}} = 32.88 \text{ rpm}$

15. A 25 kg disk with radius .5m is initially spinning with a constant angular speed of 4 rad/s. The angular speed is then increased to 8 rad/s in 5 seconds. Find the angular acceleration, the moment of inertia and the torque of the disk.

$m = 25 \text{ kg}$   
 $r = .5 \text{ m}$

$\alpha = \frac{\Delta \omega}{\Delta t} = \frac{4}{5} \text{ rad/s}^2$

$\omega_i = 4 \text{ rad/s}$

$I = \frac{1}{2} m r^2 = \frac{1}{2} (25)(.5)^2 = 3.125 \text{ kg m}^2$

$\omega_f = 8 \text{ rad/s}$

$\tau = I \alpha = 3.125(4/5) = 2.5 \text{ N}\cdot\text{m}$

$t = 5 \text{ sec}$